

$$Hf \in Hv(f)v(H)$$

2Let  $k \subseteq \mathbb{C}$  be a field and  $G$  an ordered abelian group. Let  $K = k((G))$  be the field of generalized power series endowed with the valuation  $v$ . Verify that  $v(K^\times) \cong G$ . Let  $s = \sum_{g \in G} s(g)t^g \in \mathcal{O}_v$ . Show that for the residue  $\bar{s}$  of  $s$  we have  $\bar{s} = s(v(s))$ . Conclude that

for  $\alpha \in \mathbb{R}^{>0}$  and  $(\alpha)_n := \alpha \cdot (\alpha - 1) \cdots (\alpha - n + 1)$ . Then prove that for  $\varepsilon \in \mathbb{R}$  with  $v(\varepsilon) > 0$  we have  $(1 + \varepsilon)^{\frac{1}{2}} = \sqrt{1 + \varepsilon}$ .

**Definition:**

[[a]] Let  $G$  be an abelian group and  $p \in \mathbb{N}$  prime.  $G$  is called  $p$  divisible if for every  $g \in G$  there exists  $h \in G$  such that  $g = ph$ .

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